MATH 634, Spring 2013 PRACTICE PROBLEMS in preparation for Exam 2 on Monday, May 13, 2013.

The exam covers:

- Pearls in Graph Theory, Sections 3.1, 7.2, 8.1–8.3, 9.1, 9.2, and 10.3.
- Additional topics that are included in the course notes since the first exam, including and not limited to: knight's tours, de Bruijn graphs, stable marriage algorithm, Ford-Fulkerson and related algorithms.

Below are some questions that practice concepts from the class.

- Book questions: 3.1.11, 8.1.8, 9.1.8, 9.2.2, 9.2.4 (using a theorem from Chapter 3.1)
- **Q1.** Let T be a tree and e be any edge of T. Prove that T/e (T contract e) is a tree.
- Q2. Show that the planar dual of the octohedron is the cube and vice versa.
- Q3. Show that the Petersen graph is a minor of this graph:



- **Q4.** When embedding K_6 into the torus, show that the generalization of Euler's formula holds (p q + r = 2 2g).
- **Q5.** Prove that the Gale-Shapley algorithm is female-pessimal when run with the men proposing. (Hard!)
- **Q6.** The market for kumquats is booming! Five markets (I through V) each have put orders into the five large kumquat distributors (A through E).
 - A has 5 kumpuats and can deliver to I, II, and III.
 - B has 4 kumpuats and can deliver to I, III, and IV.
 - C has 2 kumpuats and can deliver to II and III.
 - D has 5 kumpuats and can deliver to III and V.
 - E has 4 kumpuats and can deliver to IV and V.

Market I desires 5 kumquats, II desires 2, III desires 4, IV desires 6, and V desires 3. Is it possible for all the markets to receive their desired quantity of kumquats for the distributors? If so, give a valid transshipment. If not, explain why not.