

Evaluation of Mathematical Models

In what ways can a model be “good”? A model can be...

▶ **Accurate**

- ▶ Is the output of the model very near to correct?

▶ **Descriptively Realistic**

- ▶ Is the model based on assumptions which are correct?

▶ **Precise**

- ▶ Are the predictors of the model definite numbers?

▶ **Robust**

- ▶ Is the model relatively immune to errors in the input data?

▶ **General**

- ▶ Does the model apply to a wide variety of situations?

▶ **Fruitful**

- ▶ Are the conclusions useful?
- ▶ Does the model inspire other good models?

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This year, there are 5 million students. (S)

We might conjecture that in general, $S = 0.5P$.

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Model Assumption 2:

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Model Assumption 1: Each college student is in 18–22 year old range.

Model Assumption 2: One of every two is enrolled in college.

If next year there are projected to be 11,000,000 18–22 year olds, we would estimate the college population to be of size $E =$ _____.

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Otherwise, the model is **inaccurate**.

Problem:

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Question: Is this model descriptively realistic?

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Example. Full moons. A full moon appears to occur every 29 days. Let M_L , M_N be the dates of the last and next full moons. Is the model

$$M_N = M_L + 29$$

descriptively realistic? _____ Why?

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Example. A more descriptively realistic model would incorporate other age groups. Replace Assumptions 1 and 2 by:

Model Assumption 3: College students are either:

- ▶ 18–22 (P_a of these)
- ▶ 23 or older (P_b of these)
- ▶ 17 or younger (P_c of these)

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Model Assumption 4: The enrolled percentages for each age range is:

- ▶ 30% for people aged 18–22
- ▶ 3% for people aged 23 or older
- ▶ 1% for people aged 17 or younger

We would estimate the college population to be of size

$$E = 0.3P_a + 0.03P_b + 0.01P_b.$$

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Circle one: The enrollment models are precise imprecise. Why?

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Circle one: The enrollment models are precise imprecise. Why?

Keep **Assumption 1**: Each college student is in 18–22 year old range.

Revise **Assumption 2***: The percentage of 18–22 year olds in college is between 46% and 50%. (Historically)

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Model Conclusion: $(0.46)(11,000,000) \leq E \leq (0.5)(11,000,000)$
 $5,060,000 \leq E \leq 5,500,000.$

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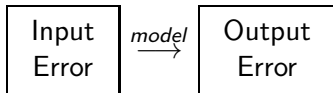
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This model is imprecise, but perhaps more helpful than the precise answer from before.

Robustness and Percentage Error

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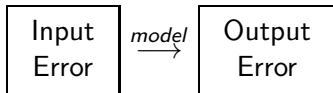
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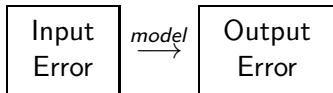


Example. If our population estimate (input) has an error of 10%, how much does our college enrollment estimate (output) change?

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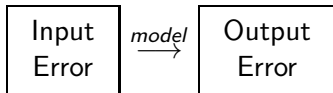
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Ask: Is the output error less than 10% or more than 10%?

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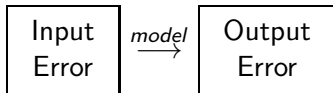
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- ▶ Some models **magnify** the errors that exist in the input data; we say these models are **sensitive to error** or **not robust**.

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Make sure we understand: What does 10% error mean?

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Example. Suppose that the census measures the 18-22 year old population to be 9,300,000 while the true population is 9,500,000.

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Most of the time, we discuss the **absolute value** of percentage error. In other words, 5% error means the error is either -5% or 5% .

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Recall: Population Estimate $P' = 11,000,000$.

Calculating the true population P based on a +5% error in P' :

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$$\begin{aligned}\frac{11,000,000 - P}{P} = 0.05 &\implies 11,000,000 - P = 0.05P \implies \\ 11,000,000 = 1.05P &\implies P = 10,475,190\end{aligned}$$

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How does this impact the true student enrollment E ?

$$E = 0.5P = 0.5(10,475,190) = 5,238,095,$$

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This highlights the principle of “Error In equals Error Out”

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Suppose that we prepare for a $\pm 10\%$ error in each population P_i , where the true values are: $P_a = 10$ mil., $P_b = 90$ mil, $P_c = 50$ mil.

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If each pop. est. P_i is a 10% **overestimate** of the true value P'_i , $P'_a = 11$, $P'_b = 99$, and $P'_c = 55$.

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Then comparing the true enrollment to the estimated enrollment E' :

$$E = 0.3(10) + 0.03(90) + 0.01(50) = 6.2$$

$$E' = 0.3(11) + 0.03(99) + 0.01(55) = 6.82$$

Percentage error: $\frac{6.82-6.2}{6.2} = \frac{.62}{6.2} = 10\%$;

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Suppose that we prepare for a $\pm 10\%$ error in each population P_i , where the true values are: $P_a = 10$ mil., $P_b = 90$ mil., $P_c = 50$ mil.

If each pop. est. P_i is a 10% **overestimate** of the true value P'_i , $P'_a = 11$, $P'_b = 99$, and $P'_c = 55$.

Then comparing the true enrollment to the estimated enrollment E' :

$$E = 0.3(10) + 0.03(90) + 0.01(50) = 6.2$$

$$E' = 0.3(11) + 0.03(99) + 0.01(55) = 6.82$$

Percentage error: $\frac{6.82-6.2}{6.2} = \frac{.62}{6.2} = 10\%$; Again _____

Alternatively, P'_a 10% **underestimate**, and P'_b , P'_c 10% **overestimate**:

$P'_a = 9$, $P'_b = 99$, and $P'_c = 55$.

$$E = 0.3(10) + 0.03(90) + 0.01(50) = 6.2$$

$$E' = 0.3(9) + 0.03(99) + 0.01(55) = 6.22$$

Percentage error: $\frac{6.22-6.2}{6.2} = \frac{.02}{6.2} = 0.3\%$.

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Suppose that Queens College has 20,000 students and suppose that Private UNnamed Kansas College has 2,000 students this year.

If the year-to-year change in 18–22 year old population is 10%, then QC would gain 2,000 students while PUNK College would gain 200.

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The projected enrollment in all colleges would be:

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It is complicated to estimate total enrollment using this model.

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This model is more general because it applies to individual colleges.

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- ▶ Its conclusions are useful.
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Example. How many automobiles would be junked in a given year?

- ▶ Cars play the role of people.
- ▶ Partitioning by age of cars gives better results

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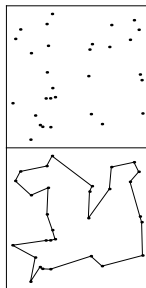
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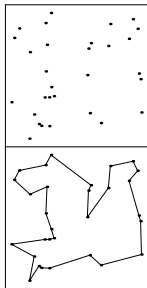
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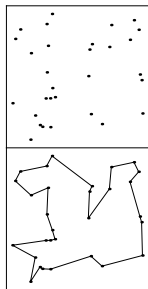
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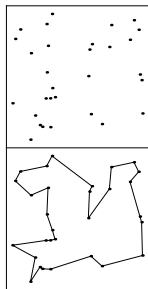
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- ▶ If you visit the same places every day, run the expensive model **once initially** in order to save money in the long run.
- ▶ If you visit different places every day, run the inexpensive algorithm daily. (Unless you're UPS or FedEx.)

